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Effect of terrain on orthometric height

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Structure of presentation



Objective:

Investigate the effect of terrain on orthometric height, within the context of the "rigorous" definition of orthometric height.

Contents:

- Show how mean value of gravity along plumbline is expressed within the "rigorous" definition of orthometric heights.
- Show numerical results.
- Review definition of orthometric heights (Helmert, Nithammer, Mader).
- Make comparisons.
- > End with concluding remarks.



Orthometric height



- Definition: length of plumbline between the geoid and the Earth's surface.
- For a numerical evaluation, knowledge of mean value of gravity along the plumbline required.
- Mean value of gravity along the plumbline is a function of mass density distribution of Earth and on shape of Earth's surface.





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Effect of topography





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Mean gravity generated by topography

> From the definition of integral mean gravity, it follows that:

$$\overline{g}^{TC}(\Omega,\rho_0) \cong \frac{1}{H(\Omega)} \left[V^{TC}(R,\Omega) - V^{TC}(R+H(\Omega),\Omega) \right]$$

> Expressed in terms of difference of potential.

$$\overline{g}^{TC}(\Omega) = \overline{g}^{TC}(\rho_0; \Omega) + \overline{g}^{TC}(\delta \rho; \Omega)$$

Contribution coming from the mean mass density plus a correction due to density variations.

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- Mean gravity generated by topography expressed in terms of potential. Solution more accurate.
- It is composed of a contribution coming from the mean mass density plus a correction due to density variations.
- ▷ Dominant term represents the change in the roughness part of the Secondary Indirect Topographical Effects keeping a direct relationship with the topography of constant density of ρ_0 , from the geoid to the surface of the earth, divided by the height of the point of interest.
- Numerical evaluation is similar to the one applied in the geoid computation, and is rather simple.





Several prescriptions:

✓ Helmert's: (1890) ✓ Niethammer: $g^{-H}(\Omega) = g(r_t(\Omega)) + \frac{\partial \gamma(H,\phi)}{\partial H} \frac{H^{O}(\Omega)}{2} - 2\pi G \rho_0 H^{O}(\Omega)$ ✓ Niethammer: $g^{-N}(\Omega) = g^{-H}(\Omega) - g^{TC}(r_t(\Omega)) + g^{TC}(\Omega)$ (1932) ✓ Mader: $g^{-M}(\Omega) = g^{-H}(\Omega) - \frac{1}{2}(g^{TC}(r_t(\Omega)) - g^{TC}(r_g,\Omega))$

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(some) Characteristics of previous approaches

- \succ ... dealing with a terrain term ...
- > Mader orthometric height:
 - \checkmark assumes linear variation in gravity above geoid.
 - ✓ uncertainty increases in mountainous area
 - computationally intensive (requires computation of terrain effects at topograpic surface and geoid)
- > Niethammer orthometric height:
 - ✓ Greater compatibility with GPS-derived heights from a gravimetric geoid that includes terrain correction.
 - \checkmark More computationally intensive than Mader's



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Concluding remarks



- Mean gravity generated by topography following from rigorous definition of orthometric height.
- Mean gravity generated by topography expressed in terms of potential
 ⇒ Solution more accurate.
- Numerical evaluation similar to the one applied in the geoid computation => more compatible with GPS heights derived from a gravimetric geoid.
- > Numerical comparison to be carried out using synthetic gravity field.